

WESTMINSTER SCHOOL THE CHALLENGE 2019

MATHEMATICS II

Tuesday 30 April 2019

Time allowed: 1 hour 30 minutes

You will need a calculator for this paper

All your working should be clearly shown.

You should attempt all the questions.

Please write in black or blue ink.

- A florist has 60 bunches of Gypsophila to sell. She sells 41 bunches for £4.30 each. Towards the end of the day she offers a discount, and sells all the remaining bunches at a reduced price. If her costs were £180 and she finished the day with a profit of £62-80, what was the reduced price per bunch?
- 2 Vehicle A travels 44 miles per gallon of fuel used. Vehicle B uses 6·3 litres of fuel per 100 km driven.

Use the conversion factors 1 mile ≈ 1.609 km; 1 gallon ≈ 4.546 litres to work out which vehicle is more efficient. Show clearly how you decide.

- 3 a i What would need to be subtracted from 5x to obtain 3x + a?
 - ii By what would you multiply $\frac{2x}{3y}$ to make $\frac{3}{y}$?
 - **b** Make L the subject of

$$K = \frac{M}{\sqrt{A-L}}$$
.

c Solve the equation

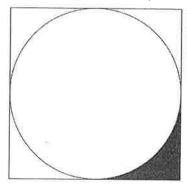
$$\frac{2}{5}(1-3x)=4-\frac{3x}{4}$$
.

d Simplify

$$5 - \frac{5(6-x)}{6}$$
.

- **4 a** The mass of a green anaconda increases by 22% each year. If the snake currently weighs 72 kg, how much did it weigh four years ago?
 - **b** The level of radiation in a nuclear fallout zone decreases by a constant percentage each year. If a radiation counter in the zone read 500 counts per minute in January 2000, and 120 counts per minute in January 2019, what would it have read in January 2012?
- Josh collects trading cards. The size of his collection grew by 14% during 2016, but it fell during 2017. During 2018, the size increased by 7%. At the end of 2018, Josh calculated that he would have to sell 9% of the collection to reduce it back to the size it was at the beginning of 2016. By what percentage did the size fall during 2017?
- The surface area of a sphere is known to be between 27.5 cm² and 28.5 cm². Show clearly that the volume of the sphere, correct to the nearest cubic centimetre, is guaranteed to be 14 cm³.

7 The diagram shows a circle fitting snugly inside a square.



- a If the circumference of the circle is 41 cm, what is the perimeter of the shaded region?
- **b** If the shaded area is 8.8 cm², what is the area of the square?
- Last week, all my Year 7 class handed in their homework and it took me an average of seven and a half minutes to mark each boy's work. All of the 18 boys in my Year 8 class handed in their homework, which took a lot longer to mark: altogether it took me 6 hours and 36 minutes to mark my Year 7 and 8 homework.

This week, four of my Year 7 class and two of my Year 8 class failed to hand in their homework. It only took me an average of six minutes to mark each Year 7 boy's work, but it took me four minutes longer than last week to mark each Year 8 boy's prep, on average. Altogether, this week's marking took twenty minutes less than last week.

How many boys are in my Year 7 class and how long did it take me on average to mark each Year 8 boy's prep last week?

The traditional English system of weights and measures includes four units of mass: the ton, the stone, the pound, and the ounce. There are 16 ounces in a pound, 14 pounds in a stone, and 160 stones in a ton.

Convert 1 234 567 ounces into the form "w tons, x stones, y pounds, and z ounces."

- 10 I have a large number of identical maths textbooks, which I am trying to stack in a rectangular space on my wall.
 - If I stack the books **upright**, as in Figure 1, I can fit 5 rows of 75, leaving a 1 cm gap along the top and right-hand edges of the space, as shown in Figure 2.

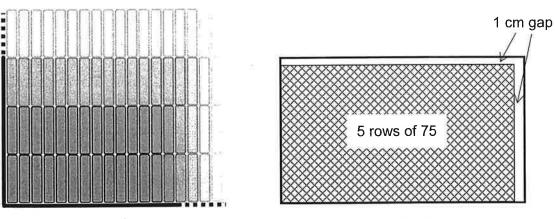
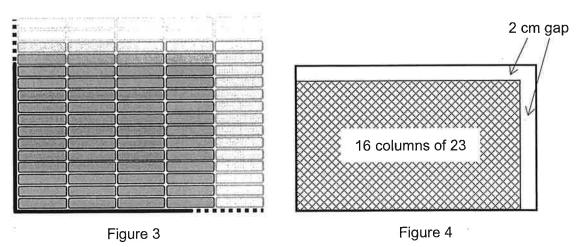


Figure 1

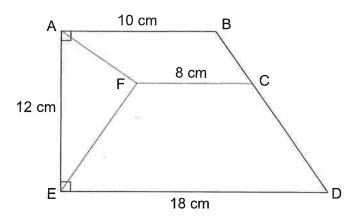
Figure 2

If I stack the books on their side, as in Figure 3, I can fit 16 columns of 23, leaving a 2 cm gap along the top and right-hand edges of the space, as shown in Figure 4.



Find the height and width of the rectangular space.

In the diagram below, AB, FC and ED are parallel, and AE is perpendicular to ED. BCD is a straight line.



Given that CDEF has three times the area of ABCF, find the area of AFE.

Stefan and Toby want to build toy spacecraft from *Astro* construction parts. Stefan wants to build an *Astro Scout*, whilst Toby wants to build an *Astro Transport*. They do not have all the parts they need, so they write down how many more of each part they will buy.

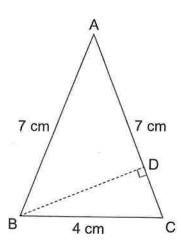
	Astro Scout	Astro Transport
Guns	17	27
Cosmic shields	8	13
Turbo engines	5	8

At the toy shop Stefan is told his extra parts will cost £53.05, and Toby is told his extra parts will cost £84.95. Each part costs a whole number of pence, and there are no discounts for bulk buying.

Which costs more, a gun or a cosmic shield, and by how much?

A prism with a volume of 963 cm³ has a right-angled triangle as its cross-section. The length of the hypotenuse of the cross-section is three times its shortest side, and the length of the prism is five times the hypotenuse of the cross-section. Find the cross-sectional area of the prism.

14 a The triangle ABC is isosceles with AB = AC = 7 cm and BC = 4 cm.



i Find the area of ABC.

The point D lies on AC such that BD is perpendicular to AC.

- ii Find the length of BD, correct to 3 significant figures.
- b A circle drawn on horizontal ground has centre O and radius 3 metres. A vertical flagpole of height 10 metres stands at O. A wire support connects F, the top of the flagpole, to G, a point on the circle's circumference. Another point H on the circle's circumference is such that angle GOH = 90°.

A strip of decorative bunting is to be added. One end will be attached to the ground at H, and the other end will be fixed to the wire support at a point X. The bunting is made as short as possible, so that angle HXF is a right angle.

Calculate the length HX.

